

Accelerated RRT* and its evaluation on Autonomous Parking

Jiri Vlasak, Michal Sojka, and Zdeněk Hanzálek

DOI: <https://doi.org/10.5220/0007679500860094>

Cite as: J. Vlasak., M. Sojka., and Z. Hanzálek. Accelerated rrt* and its evaluation on autonomous parking. In *Proceedings of the 5th International Conference on Vehicle Technology and Intelligent Transport Systems - Volume 1: VEHITS*,, pages 86–94. INSTICC, SciTePress, 2019

Source code: <http://rtime.felk.cvut.cz/gitweb/hubacj11/iamcar.git>

Accelerated RRT* and its evaluation on Autonomous Parking

Jiri Vlasak^{1,2}, Michal Sojka² and Zdeněk Hanzálek²

¹Faculty of Electrical Engineering, Czech Technical University in Prague

²Czech Institute of Informatics, Robotics and Cybernetics, Czech Technical University in Prague
{jiri.vlasak.2, michal.sojka, zdenek.hanzalek}@cvut.cz

Abstract

Finding a collision-free path for autonomous parking is usually performed by computing geometric equations, but the geometric approach may become unusable under challenging situations where space is highly constrained. We propose an algorithm based on Rapidly-Exploring Random Trees Star (RRT*), which works even in highly constrained environments and improvements to RRT*-based algorithm that accelerate computational time and decrease the final path cost. Our improved RRT* algorithm found a path for parallel parking maneuver in 95 % of cases in less than 0.15 seconds.

Keywords: Autonomous parking, Rapidly-Exploring Random Trees, Reeds and Shepp steering, Dijkstra optimization, Nearest neighbor heuristics.

1 INTRODUCTION

Modern cars are commonly equipped with parking assistants that can perform parallel or perpendicular parking maneuvers. Parking is a relatively easy task as the movement is slow and the car dynamics might be neglected. Usually, geometric equations are used for planning these maneuvers. A geometric approach has limitations when applied in unexpected environments or when more than a simple parking maneuver has to be planned. In this paper we address the cases, when more advanced planners need to be used, and one of the problems experienced by those complex planners is their computational complexity.

For this paper, we define the parking problem as finding

a collision-free path from an initial car position (i.e., x , y , and *heading*) to the goal position under the presence of an arbitrary number of known static obstacles. The path may consist of an arbitrary number of path segments alternating forward and backward drives of the car. We are interested in a close to optimal parking maneuver path in the sense of path length respecting the kinematic constraints of the car.

In this paper, we propose an RRT*-based algorithm to solve the autonomous parking problem, which we define more formally in Section 2. Contrary to well-known A* algorithm, RRT* algorithm does not need space discretization. Also, it handles nonholonomic constraints by design. The RRT* algorithm searches the state space by creating a tree structure that represents possible paths. RRT*-based algorithms were successfully applied to a wide range of planning problems from the robot, vehicle, and aerial domains. However, they were also used in not such apparent problems as tunnel detection in proteins from the field of molecular biology.

Our algorithm uses Reeds and Shepp curves for particular path segments when building the tree and Euclidean distance as a metric for the nearest neighbor search. We complemented the RRT* algorithm with an optimization procedure based on the Dijkstra algorithm used to reduce the number of the path segments and to lower the cost of the path connecting initial and goal pose.

The main contributions of this paper are:

- Minimization of the path cost with an optimization procedure based on the shortest path by Dijkstra algorithm.
- Speed up of the RRT* path search with the nearest

neighbor heuristics.

In our experiments (see Section 5), we compare multiple cost functions of the nearest neighbor search and show that the fastest approach to find the path is to use the Euclidean distance as the cost function in the nearest neighbor search (see Figure 4). We also evaluate the effectiveness of our optimization procedure based on the Dijkstra algorithm and show (see Figure 5) that it significantly improves the cost of the path even when compared to other algorithms such as RRT*-Smart. In Section 6 we summarize our results. The source code of our algorithm is available ¹.

1.1 Related Works

A common approach to solve a parking problem is to split the task to the environment detection, the path planning, and the path execution. In this paper, we consider the path planning part.

Typical parking problems can be classified into two classes: parallel parking and perpendicular parking. Some publications consider only parallel parking [Gupta et al., 2010], [Cheng et al., 2013], [Vorobieva et al., 2013], or only perpendicular parking [Petrov et al., 2015]. In this paper, we propose a universal method which considers obstacles of arbitrary shape.

Many published approaches use Reeds and Shepp curves [Reeds and Shepp, 1990] for path planning [Lee et al., 2006] without considering obstacles. In [Fraichard and Scheuer, 2004], the authors present Continuous-Curvature Paths that extend the Reeds and Shepp line segments and circular arcs with clothoid arcs. Resulting paths have continuous curvature, so a car that follows a path does not have to stop to change orientation of the wheels. Continuous-Curvature Paths have been used in [Muller et al., 2007], [Vorobieva et al., 2013], [Cheng et al., 2013], and [Yi et al., 2017]. In [Kim et al., 2010], the authors use two basic motions to create a set of motions. Finally, [Hsu et al., 2008], [Gupta et al., 2010], and [Liang et al., 2012] describe parking using paths generated with two circles geometry.

However, in real-life situations, a typical parking scenario may be disturbed by sloppy parked neighbor car,

temporary parked bike, non-standard parking slot shape, or other unspecified constraints. Therefore, when a parking slot is detected, evaluation of a situation may fail, and an approach based on geometric equations may become unusable in such a case.

In this paper, we propose RRT*-based algorithm which can handle complex parking situations. Rapidly-Exploring Random Trees (RRT) [LaValle, 1998] is a randomized algorithm that can handle nonholonomic constraints. Although RRT is probabilistically complete (with probability 1, the algorithm converges to the solution, as time tends to infinity), it is not asymptotically optimal [Karaman and Frazzoli, 2011]. Therefore, Karaman and Frazzoli proposed the RRT* algorithm, which converges to an optimal solution as time tends to infinity. In [Islam et al., 2012], the authors improved the RRT* algorithm by using path optimization and intelligent sampling and named the resulting algorithm RRT*-Smart. After the initial path is found, RRT*-Smart converges to the optimum faster than RRT*. In our approach, we stop the RRT* algorithm when a path is found, and then we optimize the path by Dijkstra algorithm.

2 THE PARKING PROBLEM

In this section, we define the problem and terminology used throughout this paper.

A *pose* is a triplet $p = (x, y, \theta)$, where x, y are cartesian coordinates and θ is a heading.

A *search space* is a set of poses $S = \{(x, y, \theta) \mid x \in [XMIN, XMAX], y \in [YMIN, YMAX], \theta \in [0, 2\pi)\}$, where $XMIN, XMAX, YMIN$, and $YMAX$ are borders of search space.

A *scenario* is a quintuple $s = (S, p_{init}, p_{goal}, O_C, O_S)$, where S is a search space, p_{init}, p_{goal} are init and goal poses, and O_C resp. O_S are sets of circle obstacles resp. line segment obstacles. We can see an example scenario with the final path connecting initial and goal pose in Figure 1. Example scenario also demonstrates segment obstacles (borders), circle obstacles, and the complex obstacle of arbitrary shape (compound of line segment obstacles).

Circle obstacle is a triplet $o_c = (x, y, r)$, where x, y are cartesian coordinates of the center, and r is the radius. *Line segment* obstacle is a quadruple $o_s = (x_1, y_1, x_2, y_2)$,

¹<http://rttime.felk.cvut.cz/gitweb/hubacj1/iamcar.git>

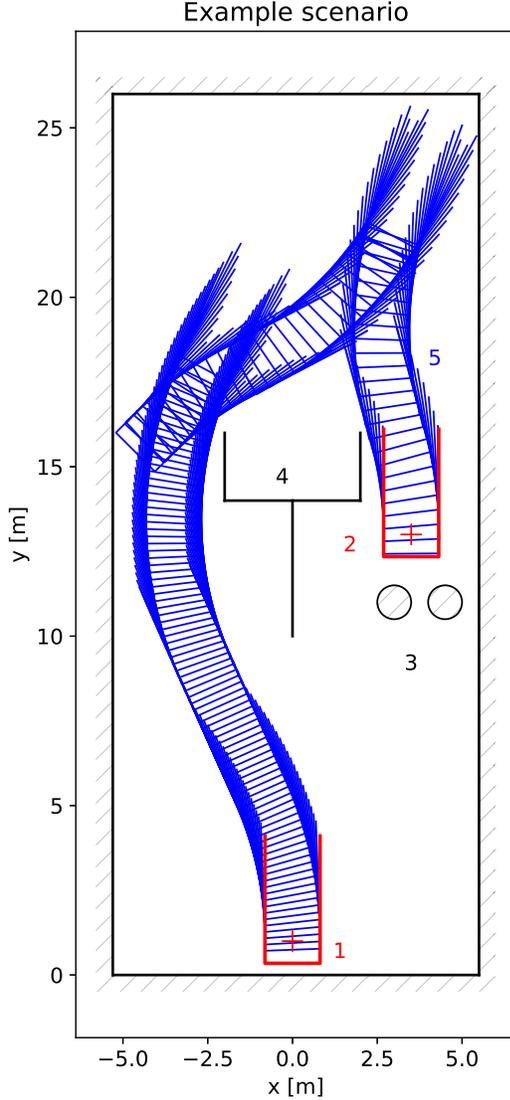


Figure 1: Example scenario with the init pose (1), the goal pose (2), two circle obstacles (3), the obstacle compound of line segment obstacles (4), and the final path (5).

where x_1, y_1 are coordinates of the line segment start and x_2, y_2 are coordinates of the line segment end.

A *car* is a quadruple $c = (l, w, R, b)$, where l is a length of the car, w is a width of the car, $R = \frac{1}{\kappa}$ is car minimum turning radius, κ is curvature, and b is car wheelbase (the distance between front and rear axles). In Figure 1, red crosses represent x, y coordinates of *init* and *goal* poses. The *U-Shape* frame represents length l , width w , and pose heading. Finally, example obstacles are hatched.

A *path* from pose a to pose b is a sequence of poses $P_{a,b} = \{p_i \mid i \in \{0, 1, \dots, n-1\}, p_0 = a, p_{n-1} = b\}$, such that P satisfies kinematic constraints given by car c .

The $collide(p, O)$ function returns *True* when a car c positioned at pose p is inside arbitrary obstacle $o \in O$, or the frame of car c collides with this obstacle. Otherwise, the function returns *False*.

The $collide(P, O)$ function returns *True* when for any pose $p \in P$ the $collide(p, O)$ returns *True*. Otherwise, the function returns *False*.

The $cost(P)$ is a *path cost* defined in Equation 1, where $RSDist(a, b)$ is Reeds & Shepp distance from pose a to pose b .

$$cost(P) = \sum_{i=0}^{i=n-2} RSDist(p_i, p_{i+1}) \quad (1)$$

We define *final path* P_F in Equation 2, where $P_{all} = \{P_{a,b} \mid a = p_{init}, b = p_{goal}, \neg collide(P, O)\}$. An example of the *final path* is in Figure 1.

$$P_F = \arg \min_{P \in P_{all}} cost(P) \quad (2)$$

3 RRT*

Rapidly-Exploring Random Tree Star (RRT*) is an asymptotically optimal randomized algorithm to solve path planning problems, such as the parking problem defined in Section 2.

RRT* uses a tree data structure that represents poses and paths, it handles nonholonomic constraints and can hold general restrictions on p_{init} and p_{goal} poses, or obstacles. Therefore, the RRT* should be able to solve the unpredictable, real-life scenarios. We can see basic RRT* pseudocode (lines 4 to 19) as part of complete RRT*-based Algorithm 1.

The fundamental element of RRT* is a *node*. The *node* is a pose extended with *parent* (the pointer to the predecessor *node*), *children* (the array of successor *nodes*), and cumulative cost $ccost = cost(P_{p_{init},node})$. As *node* is extension to pose, we may update our definition of path $P_{a,b} = \{p_i \mid i \in \{0, 1, \dots, n-1\}, p_0 = a, p_{n-1} = b\}$, such that a, b , and p_i are nodes, where p_i is parent of p_{i+1} . We use a *path* as the sequence of poses or *nodes* interchangeably.

In RRT* algorithm, all *nodes* are stored in tree data structure $\mathcal{T} = (root, V, E)$, where *root* node corresponds to p_{init} pose, V is set of nodes, E is set of edges, and $\forall n_1, n_2 \in V : \{n_1, n_2\} \in E \Leftrightarrow n_1$ is the parent of n_2 .

3.1 Basic Procedures

In this section, we describe the basic procedures of RRT* used to build \mathcal{T} data structure.

RANDOMSAMPLE procedure returns a node with a pose from search space \mathcal{S} , where x, y , and θ are randomly generated.

COST(nm, rs) function is a metric used in RRT*.

NEARESTNEIGHBOR(rs) procedure searches for a *node* with the lowest COST($node, rs$) in \mathcal{T} .

STEER(nm, rs) procedure returns a path $P_{m,rs}$. We can see the results of STEER procedure in Figure 2 (gray).

NEARNODES($ns, dist$) procedure returns a set of nodes nms from \mathcal{T} , such that $\forall n \in nms : COST(n, ns) < dist$.

CONNECT(ns, nms) procedure searches in near nodes (nms) for the best candidate node to expand \mathcal{T} towards the ns . The best candidate node is the node in \mathcal{T} that minimizes the cumulative cost of ns when it becomes the parent of the ns . The path from the best candidate node to the ns must be free of collisions. If the best candidate node is found, the na is added as a child of the best candidate node, and CONNECT(ns, nms) returns *True*. Otherwise, the procedure returns *False*.

REWIRE(ns, nms) procedure checks if for any *node* in nms there is a path with lower cumulative cost via ns . And swaps parents if so. This procedure along with CONNECT(ns, nms) ensures the asymptotical optimality of RRT*.

GOALFOUND returns *True* if $p_{goal} \in \mathcal{T}$ and *False* otherwise.

COLLIDES(na, ns) returns *True* if the path $P_{na,ns}$ collides with any obstacle of scenario, and *False* otherwise.

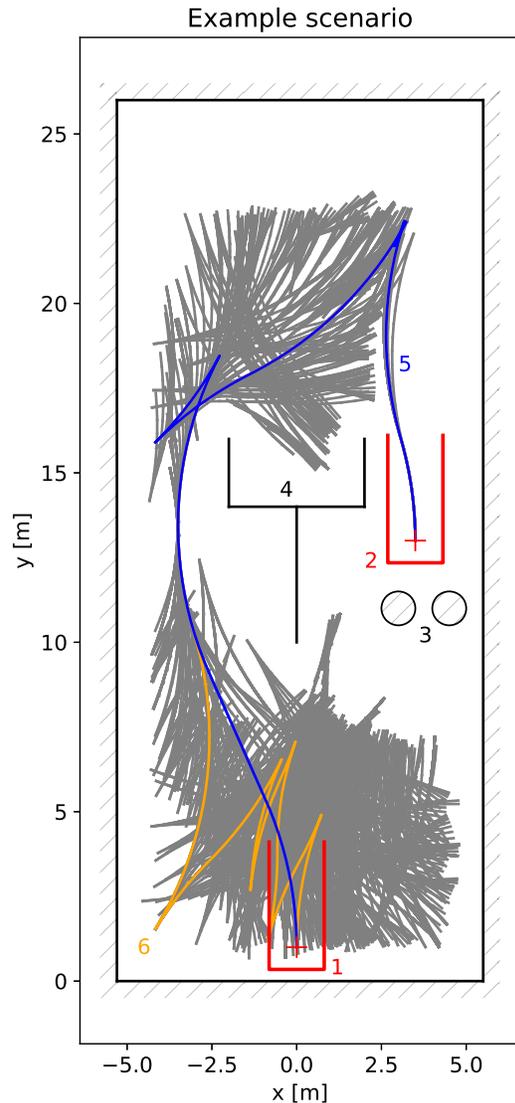


Figure 2: Example scenario with the init pose (1), the goal pose (2), two circle obstacles (3), the obstacle compound of line segment obstacles (4), the final path (5), the final path before optimization (6), and line segments and circle segments (gray).

Algorithm 1 Accelerated RRT*

```
1: Input:
   • initial pose
   • goal pose
   • array of obstacles
2: Output:
   • True if goal pose reached, False otherwise
   • array of paths connecting initial and goal pose
3: procedure RRT*
4:   while ELAPSED < TMAX do
5:      $rs \leftarrow \text{RANDOMSAMPLE}$ 
6:      $nn \leftarrow \text{NEARESTNEIGHBOR}(rs)$ 
7:      $pn \leftarrow nn$ 
8:      $newNodes \leftarrow \emptyset$ 
9:     for  $ns \leftarrow \text{STEER}(nn, rs)$  do
10:       $nns \leftarrow pn \cup \text{NEARNODES}(ns, dist)$ 
11:      if CONNECT( $ns, nns$ ) then
12:        REWIRE( $ns, nns$ )
13:         $newNodes \leftarrow newNodes \cup ns$ 
14:        if GOALFOUND then
15:          break while
16:        end if
17:         $pn \leftarrow ns$ 
18:      end if
19:    end for
20:    for  $na \leftarrow newNodes$  do
21:       $pn \leftarrow na$ 
22:      for  $ns \leftarrow \text{STEER}(na, goal)$  do
23:        if COLLIDE( $pn, ns$ ) then
24:          break
25:        end if
26:         $pn.children \leftarrow pn.children \cup ns$ 
27:        if GOALFOUND then
28:          break while
29:        end if
30:         $pn \leftarrow ns$ 
31:      end for
32:    end for
33:  end while
34:  if GOALFOUND then
35:    OPTPATH
36:  end if
37:  return GOALFOUND
38: end procedure
```

3.2 Implementation

Our RANDOMSAMPLE procedure samples randomly from the whole space S (including obstacles). We use OMPL [Sucan et al., 2012] implementation of Reeds and Shepp [Reeds and Shepp, 1990] optimal paths for STEER and COST functions. NEARNODES, CONNECT and REWIRE procedures work the same as in [Karaman and Frazzoli, 2011].

For two nodes we implemented auxiliary ISNEAR(n_1, n_2) function that returns *True* if n_1 is within the predefined Euclidean distance from n_2 ($GFDIST$) and the difference between headings of n_1 and n_2 is less than the specified angle ($GFANGLE$). We use this function to specify if the goal was found, the STEER procedure reached rs , or if two nodes are the same. For computational experiments in Section 5, we used $GFDIST = 0.05$ and $GFANGLE = \frac{\pi}{32}$.

In each iteration of RRT*-based algorithm, there is an expansion of \mathcal{T} towards the p_{goal} (see lines 20 to 32 in Algorithm 1) as used in [Kuwata et al., 2008]. We added path optimization procedure to RRT*-based algorithm (see line 35 in Algorithm 1) that is run when the goal is found as explained in Section 4.2. We can see an example of optimized final path (5) and final path before optimization (6) in Figure 2.

4 RRT* IMPROVEMENTS

In this section, we introduce our improvement to nearest neighbor search and details about path optimization procedure.

4.1 Nearest Neighbor

Because the nearest neighbor procedure returns a node with the lowest cost, such a node is a good candidate for tree expansion. The pseudocode of the nearest neighbor search is outlined in Algorithm 2. To improve the performance of finding the nearest neighbor, we use a *nodes* data structure (the array of linked lists of nodes) defined in line 3. The *nodes* data structure allows us to split search space S along the y -axis (y – axis suits better for parallel parking scenario we experimented with in Section 5), so we can compare nodes within multiples of $IYSTEP$ (in-

Algorithm 2 Nearest neighbor search

```
1: IYSIZE ▷ nn structure size
2: IYSTEP ▷ increment distance
3: nodes[IYSIZE] ▷ array of lists of nodes
4:
5: Input:
   • node to be added to data structure
6: Output:
   • data structure of nodes
7: procedure ADDIY(node)
8:    $iy \leftarrow \lfloor \frac{node.y}{IYSTEP} \rfloor$ 
9:    $nodes[iy] \leftarrow nodes[iy] \cup node$ 
10: end procedure
11:
12: Input:
   • node to be searched
13: Output:
   • the nearest neighbor of node
14: procedure NEARESTNEIGHBOR(node)
15:    $iy \leftarrow \lfloor \frac{node.y}{IYSTEP} \rfloor$ 
16:    $nn \leftarrow NULL$  ▷ nearest neighbor
17:    $c_{min} \leftarrow \infty$  ▷ minimum cost
18:    $as \leftarrow 0$  ▷ array step
19:   while  $c_{min} > as \cdot IYSTEP$  do
20:      $i \leftarrow \max(iy - as, 0)$ 
21:      $j \leftarrow \min(iy + as, IYSIZE - 1)$ 
22:     for  $n \in nodes[i] \cup nodes[j]$  do
23:       if  $EDIST(n, node) < c_{min}$  then
24:          $c_{min} \leftarrow EDIST(n, node)$ 
25:          $nn \leftarrow n$ 
26:       end if
27:     end for
28:      $as \leftarrow as + 1$ 
29:   end while
30: end procedure
```

crement distance based on *nodes* data structure) constant first.

Lines 7 to 10 describes how a *node* is added to *nodes*. First, we compute the index of *nodes* array (*iy*) where the *node* should be stored. Then, the *node* is added to the list of nodes at that *iy* index.

When looking for the nearest neighbor of the *node* in the indexing structure (lines 14 to 30), we compute *iy* index again. Then, we search the list of nodes stored in the array *nodes* on index *iy* (*nodes*[*iy*]). Finally, we repeatedly widen the interval of indexes to be investigated while the minimum cost is higher than half of the interval width times *IYSTEP* and search the lists of nodes stored in the array on indexes corresponding to the widened interval.

We use Euclidean distance as the cost function in the nearest neighbor search in contrast to Reeds and Shepp path length as the cost function for building RRT*. This approach speeds up the process but does not influence the final path cost as discussed in Section 5.

4.2 Path Optimization

The path optimization procedure is run when the goal is found. Even that RRT* is asymptotically optimal, it converges to the optimal solution very slowly. When the p_{goal} is reached for the first time a final path P_F is probably far from optimum in the sense of cost (we use Reeds and Shepp path length as cost). The purpose of path optimization procedure is to decrease the final path cost.

A final path P_F consists of topologically ordered nodes (see definition of a path in Section 2). We select *tip* nodes from the final path that are also topologically ordered. In our case, *tip* nodes are cusp nodes (nodes where the direction of movement changes) along with p_{init} and p_{goal} .

In Algorithm 3 we initialize *tip* nodes and priority queue in lines 4 to 6. In lines 7 to 28, we use Dijkstra algorithm to find the shortest path from the first *tip* node (p_{init}) to the last one (p_{goal}). From the priority queue, we pop the node n_i (where i is the index of n_i node in *tips* array) with the lowest cumulative cost. Then, we call STEER(n_i, n_j) procedure from n_i to all n_j for $j > i$ (see lines 12 to 27) that returns path P_{n_i, n_j} . If P_{n_i, n_j} is collision free and cumulative cost of n_j is smaller when reached via P_{n_i, n_j} then parent and cumulative cost of n_j are updated, and n_j is pushed to the priority queue if not visited

Algorithm 3 Path optimization

```
1: Input:
   • path connecting initial and goal pose
2: Output:
   • lower cost path connecting initial and goal pose
3: procedure OPTPATH
4:    $tips \leftarrow$  cusp nodes ▷ array
5:    $pq \leftarrow \emptyset$  ▷ priority queue
6:    $pq \leftarrow pq \cup tips[0]$ 
7:   while  $|pq| \neq 0$  do
8:      $n_i \leftarrow \text{POP}(pq)$ 
9:     if  $n_i = tips[\text{SIZE}(tips) - 1]$  then
10:      break
11:    end if
12:    for all  $j > i$  do
13:       $n_j \leftarrow tips[j]$ 
14:       $P_{n_i, n_j} \leftarrow \text{STEER}(n_i, n_j)$ 
15:       $c \leftarrow n_i.ccost + \text{COST}(n_i, n_j)$ 
16:      if  $\text{COLLIDE}(n_i, n_j)$  then
17:        continue
18:      end if
19:      if  $c < n_j.ccost$  then
20:         $n_j.ccost \leftarrow c$ 
21:         $n_j.parent \leftarrow i$ 
22:        if  $n_j.visited = \text{False}$  then
23:           $n_j.visited \leftarrow \text{True}$ 
24:           $pq \leftarrow pq \cup n_j$ 
25:        end if
26:      end if
27:    end for
28:  end while
29:   $opath \leftarrow \emptyset$  ▷ new optimized path
30:   $i \leftarrow \text{SIZE}(tips) - 1$ 
31:  while  $i > 0$  do
32:     $opath \leftarrow opath \cup tips[i]$ 
33:     $i \leftarrow tips[i].parent$ 
34:  end while
35:   $opath \leftarrow opath \cup tips[0]$ 
36:  if better cost of  $opath$  then
37:    return True
38:  end if
39:  return False
40: end procedure
```

already. The process repeats until the priority queue is empty or $n_i = p_{goal}$.

Optimized path found by Dijkstra is retrieved in lines 29 to 35. If the cumulative cost of p_{goal} is better, OPTPATH procedure returns *True* and *False* otherwise.

5 COMPUTATIONAL EXPERIMENTS AND EVALUATION

We present the results of computational experiments for parallel parking scenario with no obstacle in Section 5.1, and the results of computational experiments for parallel parking scenarios with circle obstacle in Section 5.2.

We are interested in the *nearest neighbor* search and *path optimization* procedures. Specifically, we are interested in how does the cost function, used in the nearest neighbor search, influences algorithm computation time. We experimented with the following implementations of the nearest neighbor search:

- Nearest neighbor search with the cost based on Reeds and Shepp path length.
- Nearest neighbor search with the cost based on Reeds and Shepp path length but with the heading of nodes temporarily set to the same value.
- Nearest neighbor search with the cost based on Euclidean distance.

Also, we would like to know if the path optimization procedure influences the cost of the final path. We tested the following path optimization possibilities:

- No path optimization.
- Path optimization from [Islam et al., 2012].
- Path optimization described in Algorithm 3.

The car we use for experiments is 1.625 m wide and 3.760 m long. The minimum turning radius of the car is 10.820 m and wheelbase is 2.450 m.

We run computational experiments on a single core of Intel(R) Core(TM) i7-5600U CPU @ 2.60 GHz with MemTotal: 16322516 kB.

5.1 Scenario with No Obstacle

We tested RRT*-based algorithm on parallel parking scenario shown in Figure 3. The parking lot is 2.2 m wide and 6.5 m long [CSN 73 6056, 2011]. The width of the street is 2.75 m.

We let the Algorithm 1 to run for up to 10 seconds. When the RRT*-based algorithm finds the goal, the OPT-PATH procedure optimizes the final path. We repeated the experiment 10000 times for this scenario.

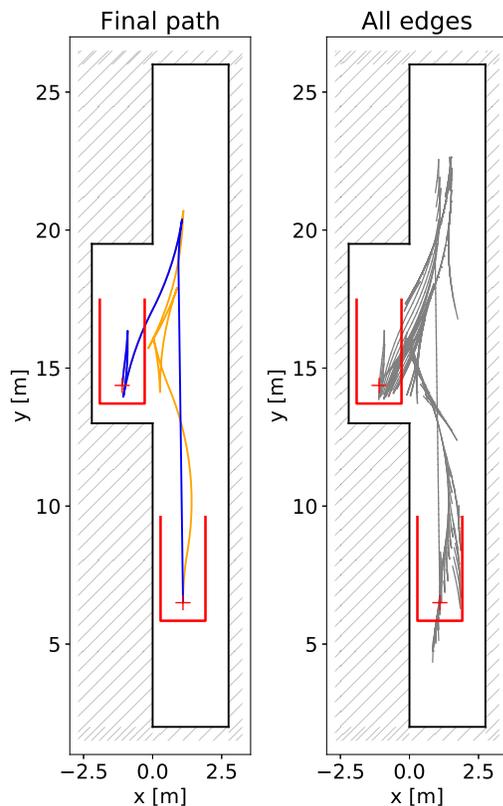


Figure 3: Parallel parking scenario with no obstacle. On the left, there is a final path before optimization (orange) and optimized final path (blue). On the right, there is a complete tree of all paths (gray).

5.1.1 Nearest Neighbor Search

We compare the computation times when the algorithm found the final path for different cost functions used in the nearest neighbor search implementations. We can see the results in the histogram with the logarithmic scale in Figure 4.

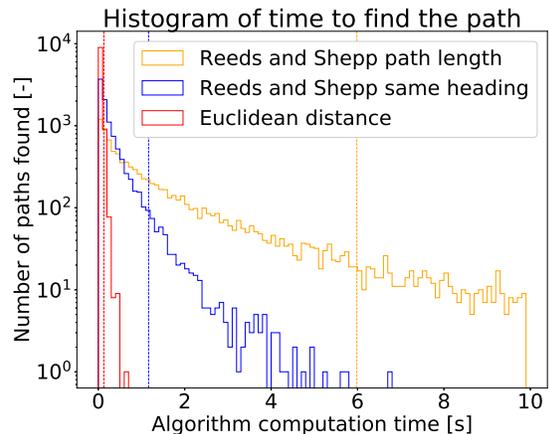


Figure 4: Histogram of time to find the path. Vertical dashed lines represent 95 % percentile (red is 0.13, blue is 1.16, orange is 5.98).

For the nearest neighbor search implementation with the Reeds and Shepp cost function (the same cost function used for building \mathcal{T} , orange in Figure 4), the algorithm did not find the goal in all runs. On the other hand, for the nearest neighbor search implementation where we used the Euclidean distance as the cost function (red in Figure 4), the goal was found in 100 % of runs. For comparison purposes, we run the experiment for the nearest neighbor search implementation with Reeds and Shepp cost function, where the heading of the nodes was temporarily set to the same value (blue in Figure 4).

5.1.2 Path Optimization

We also compared the final path costs for different path optimization procedures. We can see the results in the histogram with the logarithmic scale in Figure 5.

We can see the improvement over no path optimization (orange) when algorithm from [Islam et al., 2012] is used

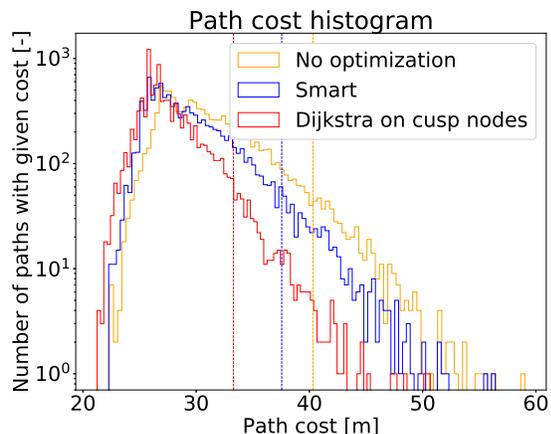


Figure 5: Path cost histogram. Vertical dashed lines represent 95 % percentile (red is 33.29, blue is 37.56, orange is 40.31).

(blue). And we can see that the path optimization from Algorithm 3 (red) has the best results.

5.2 Scenario with Circle Obstacle

Further, we tested RRT*-based algorithm on parallel parking scenarios shown in Figure 6. The parking lot is 2.2 m wide and 6.5 m long [CSN 73 6056, 2011]. The width of the street is 2.75 m. There is a random circle obstacle with diameter of 0.5 m laying on the street near the parking lot.

We let the Algorithm 1 to run for up to 10 seconds. When the RRT*-based algorithm finds the goal, the OPT-PATH procedure optimizes the final path. We repeated the experiment 10000 times for this scenario.

The results are similar to the results in Section 5.1. The cost based on the Euclidean distance speeds up the algorithm computation time (95 % percentile), dependent on the obstacle position, to 0.12 s for Scenario 1 and to 0.66 s for Scenario 2. The path optimization procedure decreases the cost of the final path (95 % percentile) by 4 % concerning No optimization case for both scenarios.

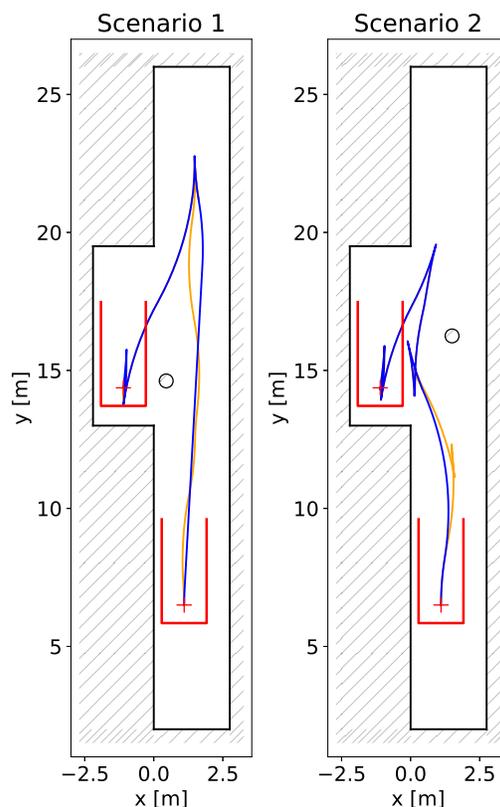


Figure 6: Parallel parking scenarios with circle obstacle. Scenarios 1 and 2 differ in the position of circle obstacle. There is the final path before optimization (orange) and the optimized final path (blue).

6 CONCLUSION

We proposed the RRT*-based algorithm for planning parking paths and experimented with the nearest neighbor search and path optimization procedures.

RRT*-based algorithm without improvements uses the cost function based on the Reeds and Shepp path length in the nearest neighbor search (as well as for building the \mathcal{T} data structure), and no optimization procedure. Our improvements include the cost function based on Euclidean distance in the nearest neighbor search and optimization procedure based on the Dijkstra algorithm.

We have shown that when we use the cost function based on the Reeds and Shepp path length for building the \mathcal{T} data structure and the cost function based on the Euclidean distance in the nearest neighbor search, there is a significant acceleration in algorithm computation time.

Additionally, we have shown that the path optimization procedure based on the Dijkstra algorithm for the shortest path search can optimize the final path to 63 % of the original cost in 95 % of cases, for the parallel parking scenario without obstacles, which is a better result than the optimization procedure used in [Islam et al., 2012]. However, for parallel parking scenario with circle obstacle, the optimized cost is only 96 % of the original cost in 95 % of cases.

Finally, from the experiments we can see that for parallel parking scenario with no obstacle, RRT*-based algorithm with improvements tends to significantly faster computation time as well as to lower final path cost. However, for parallel parking scenario with circle obstacle, RRT*-based algorithm with improvements tends to significantly faster computation time but about 10 % to 20 % worse final path cost than RRT*-based algorithm without improvements.

In our future work, we are going to experiment with the improvements presented in this paper. Particularly, the recognition and selection of *tip* nodes seem to be interesting. Also, the bidirectional RRT* algorithms, such as [Jordan and Perez, 2013] and [Klemm et al., 2015], could lead to significant improvements in the matter of computational time.

ACKNOWLEDGEMENTS

This work was supported by the Technology Agency of the Czech Republic under the Centre for Applied Cybernetics TE01020197.

References

- [Cheng et al., 2013] Cheng, K., Zhang, Y., and Chen, H. (2013). Planning and control for a fully-automatic parallel parking assist system in narrow parking spaces. In *Proc. IEEE Intelligent Vehicles Symp. (IV)*, pages 1440–1445.
- [CSN 73 6056, 2011] CSN 73 6056 (2011). Parking areas for road vehicles. Technical report, Praha.
- [Fraichard and Scheuer, 2004] Fraichard, T. and Scheuer, A. (2004). From reeds and shepp’s to continuous-curvature paths. 20(6):1025–1035.
- [Gupta et al., 2010] Gupta, A., Divekar, R., and Agrawal, M. (2010). Autonomous parallel parking system for ackerman steering four wheelers. In *Proc. IEEE Int. Conf. Computational Intelligence and Computing Research*, pages 1–6.
- [Hsu et al., 2008] Hsu, T., Liu, J., Yu, P., Lee, W., and Hsu, J. (2008). Development of an automatic parking system for vehicle. In *Proc. IEEE Vehicle Power and Propulsion Conf.*, pages 1–6.
- [Islam et al., 2012] Islam, F., Nasir, J., Malik, U., Ayaz, Y., and Hasan, O. (2012). RRT*-Smart: Rapid convergence implementation of RRT* towards optimal solution. In *Proc. IEEE Int. Conf. Mechatronics and Automation*, pages 1651–1656.
- [Jordan and Perez, 2013] Jordan, M. and Perez, A. (2013). Optimal bidirectional rapidly-exploring random trees.
- [Karaman and Frazzoli, 2011] Karaman, S. and Frazzoli, E. (2011). Sampling-based algorithms for optimal motion planning. *The international journal of robotics research*, 30(7):846–894.
- [Kim et al., 2010] Kim, D., Chung, W., and Park, S. (2010). Practical motion planning for car-parking control in narrow environment. *IET Control Theory Applications*, 4(1):129–139.
- [Klemm et al., 2015] Klemm, S., Oberlinder, J., Hermann, A., Roennau, A., Schamm, T., Zollner, J. M., and Dillmann, R. (2015). Rrt *-connect: Faster, asymptotically optimal motion planning. In *Proc. IEEE Int. Conf. Robotics and Biomimetics (ROBIO)*, pages 1670–1677.
- [Kuwata et al., 2008] Kuwata, Y., Fiore, G. A., Teo, J., Frazzoli, E., and How, J. P. (2008). Motion planning for urban driving using rrt. In *Proc. IEEE/RSJ Int. Conf. Intelligent Robots and Systems*, pages 1681–1686.
- [LaValle, 1998] LaValle, S. M. (1998). Rapidly-exploring random trees: A new tool for path planning.
- [Lee et al., 2006] Lee, K., Kim, D., Chung, W., Chang, H. W., and Yoon, P. (2006). Car parking control using a trajectory tracking controller. In *Proc. SICE-ICASE Int. Joint Conf.*, pages 2058–2063.
- [Liang et al., 2012] Liang, Z., Zheng, G., and Li, J. (2012). Automatic parking path optimization based on bezier curve fitting. In *Proc. IEEE Int. Conf. Automation and Logistics*, pages 583–587.
- [Muller et al., 2007] Muller, B., Deutscher, J., and Grodde, S. (2007). Continuous curvature trajectory design and feedforward control for parking a car. 15(3):541–553.
- [Petrov et al., 2015] Petrov, P., Nashashibi, F., and Marouf, M. (2015). Path planning and steering control for an automatic perpendicular parking assist system. In *7th Workshop on Planning, Perception and Navigation for Intelligent Vehicles, PPNIV*, volume 15, pages 143–148.
- [Reeds and Shepp, 1990] Reeds, J. and Shepp, L. (1990). Optimal paths for a car that goes both forwards and backwards. *Pacific journal of mathematics*, 145(2):367–393.
- [Sucan et al., 2012] Sucan, I. A., Moll, M., and Kavraki, L. E. (2012). The open motion planning library. *IEEE Robotics Automation Magazine*, 19(4):72–82.
- [Vorobieva et al., 2013] Vorobieva, H., Minoiu-Enache, N., Glaser, S., and Mammar, S. (2013). Geometric continuous-curvature path planning for automatic parallel parking. In *Proc. SENSING AND CONTROL (ICNSC) 2013 10th IEEE INTERNATIONAL CONFERENCE ON NETWORKING*, pages 418–423.
- [Yi et al., 2017] Yi, Y., Lu, Z., Xin, Q., Jinzhou, L., Yijin, L., and Jianhang, W. (2017). Smooth path planning for autonomous parking system. In *Proc. IEEE Intelligent Vehicles Symp. (IV)*, pages 167–173.